

$$\int_a^b \underbrace{f(x)}_u \underbrace{g'(x) dx}_{dv} = \underbrace{f(x)}_u \underbrace{g(x)}_v \Big|_a^b - \int_a^b \underbrace{g(x)}_v \underbrace{f'(x) dx}_{du}$$

Example:-

$$\int_0^1 x \tan x \, dx = \begin{cases} u = x \tan x & dv = dx \\ du = \frac{1}{1+x^2} dx & v = x \end{cases}$$

$$= x \tan x \Big|_0^1 - \int_0^1 \frac{x}{1+x^2} dx$$

$$= \left(1 \cdot \tan 1 - 0 \cdot \tan 0 \right) - \int_0^1 \frac{x}{1+x^2} dx$$

$$= \frac{\pi}{4} - \int_0^1 \frac{x}{1+x^2} dx \quad \begin{cases} u = 1+x^2 & x=0 \rightarrow u=1 \\ du = 2x dx & x=1 \rightarrow u=2 \end{cases}$$

$$= \frac{\pi}{4} - \frac{1}{2} \int_1^2 \frac{1}{u} du = \frac{\pi}{4} - \frac{1}{2} \ln|u| \Big|_1^2$$

$$= \frac{\pi}{4} - \frac{1}{2} \left(\ln 2 - \underbrace{\ln 1}_0 \right) = \frac{\pi}{4} - \frac{\ln 2}{2}$$