## Closure in Valuation: Estimating Terminal Value

In the previous chapter, we examined the determinants of expected growth. Firms that reinvest substantial portions of their earnings and earn high returns on these investments should be able to grow at high rates. But for how long? This chapter brings closure to firm valuation by considering this question.

As a firm grows, it becomes more difficult for it to maintain high growth and it eventually will grow at a rate less than or equal to the growth rate of the economy in which it operates. This growth rate, labeled stable growth, can be sustained in perpetuity, allowing us to estimate the value of all cash flows beyond that point as a terminal value for a going concern. The key question that we confront is the estimation of when and how this transition to stable growth will occur for the firm that we are valuing. Will the growth rate drop abruptly at a point in time to a stable growth rate or will it occur more gradually over time? To answer these questions, we will look at a firm's size (relative to the market that it serves), its current growth rate, and its competitive advantages.

We also consider an alternate route, which is that firms do not last forever and that they will be liquidated at some point in the future. We will consider how best to estimate liquidation value and when it makes more sense to use this approach rather than the going concern approach.

## CLOSURE IN YALUATION

Since you cannot estimate cash flows forever, you generally impose closure in discounted cash flow valuation by stopping your estimation of cash flows sometime in the future and then computing a terminal value that reflects the value of the firm at that point.

$$
\text { Value of a firm }=\sum_{t=1}^{t=n} \frac{C F_{t}}{\left(1+k_{c}\right)^{t}}+\frac{\text { Terminal value }_{n}}{\left(1+k_{c}\right)^{n}}
$$

You can find the terminal value in one of three ways. One is to assume a liquidation of the firm's assets in the terminal year and estimate what others would pay for the assets that the firm has accumulated at that point. The other two approaches value the firm as a going concern at the time of the terminal value estimation. One applies a multiple to earnings, revenues, or book value to estimate the value in the
terminal year. The other assumes that the cash flows of the firm will grow at a constant rate forever-a stable growth rate. With stable growth, the terminal value can be estimated using a perpetual growth model.

## Liquidation Value

In some valuations, we can assume that the firm will cease operations at a point in time in the future and sell the assets it has accumulated to the highest bidders. The estimate that emerges is called a liquidation value. There are two ways in which the liquidation value can be estimated. One is to base it on the book value of the assets, adjusted for any inflation during the period. Thus, if the book value of assets 10 years from now is expected to be $\$ 2$ billion, the average age of the assets at that point is five years and the expected inflation rate is 3 percent, the expected liquidation value can be estimated as:

Expected liquidation value $=$ Book value of assets ${ }_{\text {sem vear }}(1+\operatorname{Inflation~rate~})^{\text {average ifir of assets }}$ $=\$ 2$ billion $(1.03)^{5}=\$ 2.319$ billion

The limitation of this approach is that it is based on accounting book value and does not reflect the earning power of the assets.

The alternative approach is to estimate the value based on the earning power of the assets. To make this estimate, we would first have to estimate the expected cash flows from the assets and then discount these cash flows back to the present, using an appropriate discount rate. In the example above, for instance, if we assumed that the assets in question could be expected to generate $\$ 400$ million in after-tax cash flows for 15 years (after the terminal year) and the cost of capital was 10 percent, our estimate of the expected liquidation value would be:

$$
\begin{aligned}
\text { Expected liquidation value } & =\$ 400 \text { million(PV of annuity, } 15 \text { years @ } 10 \%) \\
& =\$ 3.042 \text { billion }
\end{aligned}
$$

When valuing equity, there is one additional step that needs to be taken. The estimated value of debt outstanding in the terminal year has to be subtracted from the liquidation value to arrive at the liquidation proceeds for equity investors.

## Multiple Approach

In this approach, the value of a firm in a future year is estimated by applying a multiple to the firm's earnings or revenues in that year. For instance, a firm with expected revenues of $\$ 6$ billion 10 years from now will have an estimated terminal value in that year of $\$ 12$ billion, if a value-to-sales multiple of 2 is used. If valuing equity, we use equity multiples such as price-earnings ratios to arrive at the terminal value.

While this approach has the virtue of simplicity, the multiple has a huge effect on the final value and where it is obtained can be critical. If, as is common, the multiple is estimated by looking at how comparable firms in the business today are priced by the market, the valuation becomes a relative valuation, rather than a discounted cash flow valuation. If the multiple is estimated using fundamentals, it converges on the stable growth model that will be described in the next section.

All in all, using multiples to estimate terminal value, when those multiples are estimated from comparable firms, results in a dangerous mix of relative and discounted cash flow valuation. While there are advantages to relative valuation, and we will consider these in a later chapter, a discounted cash flow valuation should provide you with an estimate of intrinsic value, not relative value. Consequently, the only consistent way of estimating terminal value in a discounted cash flow model is to use either a liquidation value or to use a stable growth model.

## Stable Growth Model

In the liquidation value approach, you are assuming that your firm has a finite life and that it will be liquidated at the end of that life. Firms, however, can reinvest some of their cash flows back into new assets and extend their lives. If you assume that cash flows, beyond the terminal year, will grow at a constant rate forever, the terminal value can be estimated as follows:

$$
\text { Terminal value }_{t}=\text { Cash flow }_{\mathrm{r}+1} /(\mathrm{r}-\text { Stable growth })
$$

The cash flow and the discount rate used will depend on whether you are valuing the firm or valuing equity. If we are valuing equity, the terminal value of equity can be written as:

$$
\text { Terminal value of } \text { equity }_{n}=\text { Cash flow to equity } y_{n+1} /\left(\text { Cost of equity } y_{n+1}-g_{n}\right)
$$

The cash flow to equity can be defined strictly as dividends (in the dividend discount model) or as free cash flow to equity. If valuing a firm, the terminal value can be written as:

$$
\text { Terminal value }_{n}=\text { Free cash flow to firm } n+1 /\left(\text { Cost of capital } l_{n+1}-g_{n}\right)
$$

where the cost of capital and the growth rate in the model are sustainable forever.
In this section, we will begin by considering how high a stable growth rate can be, how to best estimate when your firm will be a stable growth firm, and what inputs need to be adjusted as a firm approaches stable growth.

Constralnts on Stable Growth Of all the inputs into a discounted cash flow valuation model, none can affect the value more than the stable growth rate. Part of the reason for it is that small changes in the stable growth rate can change the terminal value significantly, and the effect gets larger as the growth rate approaches the discount rate used in the estimation. Not surprisingly, analysts often use it to alter the valuation to reflect their biases.

The fact that a stable growth rate is constant forever, however, puts strong constraints on how high it can be. Since no firm can grow forever at a rate higher than the growth rate of the economy in which it operates, the constant growth rate cannot be greater than the overall growth rate of the economy. In making a judgment on what the limits on stable growth rate are, we have to consider the following three questions:

1. Is the company constrained to operate as a domestic company, or does it operate (or have the capacity to operate) multinationally? If a firm is a purely domestic company, either because of internal constraints (such as those imposed by management) or external (such as those imposed by a government), the growth rate in the domestic economy will be the limiting value. If the company is a multinational or has aspirations to be one, the growth rate in the global economy (or at least those parts of the globe that the firm operates in) will be the limiting value. Note that the difference will be small for a U.S. firm, since the U.S economy still represents a large portion of the world economy. It may, however, mean that you could use a stable growth rate that is slightly higher (say 0.5 to 1 percent) for a Coca-Cola than for a Consolidated Edison.
2. Is the valuation being done in nominal or real terms? If the valuation is a nominal valuation, the stable growth rate should also be a nominal growth rate (i.e., include an expected inflation component). If the valuation is a real valuation, the stable growth rate will be constrained to be lower. Again, using CocaCola as an example, the stable growth rate can be as high as 5.5 percent if the valuation is done in nominal U.S. dollars but only 3 percent if the valuation is done in real dollars.
3. What currency is being used to estimate cash flows and discount rates in the valuation? The limits on stable growth will vary depending on what currency is used in the valuation. If a high-inflation currency is used to estimate cash flows and discount rates, the stable growth rate will be much higher, since the expected inflation rate is added on to real growth. If a low-inflation currency is used to estimate cash flows, the stable growth rate will be much lower. For instance, the stable growth rate that would be used to value Titan Cement, the Greek cement company, will be much higher if the valuation is done in drachmas than in euros.

While the stable growth rate cannot exceed the growth rate of the economy in which a firm operates, it can be lower. There is nothing that prevents us from assuming that mature firms will become a smaller part of the economy and it may, in fact, be the more reasonable assumption to make. Note that the growth rate of an economy reflects the contributions of both young, highergrowth firms and mature, stable-growth firms. If the former grow at a rate much higher than the growth rate of the economy, the latter have to grow at a rate that is lower.

Setting the stable growth rate to be less than or equal to the growth rate of the economy is not only the consistent thing to do but it also ensures that the growth rate will be less than the discount rate. This is because of the relationship between the riskless rate that goes into the discount rate and the growth rate of the economy. Note that the riskless rate can be written as:

$$
\text { Nominal riskless rate }=\text { Real riskless rate }+ \text { Expected inflation rate }
$$

In the long term, the real riskless rate will converge on the real growth rate of the economy, and the nominal riskless rate will approach the nominal growth rate of the economy. In fact, a simple rule of thumb on the stable growth rate is that it generally should not exceed the riskless rate used in the valuation.

## CAN THE STABLE GROWTH RATE BE NEGATIVE?

The previous section noted that the stable growth rate has to be less than or equal to the growth rate of $t$ reason why not since the ters firm with $\$ 100$ million in aft ny. But can it be negative? Th e can still be estimated. For in h flows growing at $-5 \%$ a yea and a cost of capital of 10 percent has a value of:

$$
\text { Value of firm }=100(1-.05) /[.10-(-.05)]=\$ 633 \text { million }
$$

Intuitively, though, what does a negative growth rate imply? It essentrally allows a firm to partially liquidate itself each year until it just about disappears. Thus, it is an intermediate choice between complete liquidation and the going concern that gets larger each year forever.
may be the right choice to make when valuing firms in industries that phased out because of technological advances (such as the manufacTriens of typewriters, with the advent of the personal computer) or where an external and critical customer is scaling back purchases for the long term (as was the ase with lefense contractors a fiter the etd of the cold war).

Key Assumptlons about 8table Growth In every discounted cash flow valuation, there are three critical assumptions you need to make on stable growth. The first relates to when the firm that you are valuing will become a stable growth firm, if it is not one already. The second relates to what the characteristics of the firm will be in stable growth, in terms of return on investments and costs of equity and capital. The final assumption relates to how the firm that you are valuing will make the transition from high growth to stable growth.

Length of the High Growth Period The question of how long a firm will be able to sustain high growth is perhaps one of the more difficult questions to answer in a valuation, but two points are worth making. One is that it is not a question of whether but when firms hit the stable growth wall. All firms ultimately become stable growth firms, in the best case, because high growth makes a firm larger, and the firm's size will eventually become a barrier to further high ${ }^{4}$ growth. In the worst-case scenario, firms may not survive and will be liquidated. The second is that high growth in valuation, or at least high growth that creates value, ${ }^{1}$ comes from firms earning excess returns on their marginal investments. In other words, increased value comes from firms having a return on capital that is well in excess of the cost of capital (or a return on equity that exceeds the cost of equity). Thus, when you assume that a firm will experience high growth for the next 5 or 10 years, you are also implicitly assuming that it will earn excess returns (over and above the required return) during that period. In a competitive market, these excess returns will eventually draw in new competitors, and the excess returns will disappear.

[^0]You should look at three factors when considering how long a firm will be able to maintain high growth.

1. Size of the firm. Smaller firms are much more likely to earn excess returns and maintain these excess returns than otherwise similar larger firms. This is because they have more room to grow and a larger potential market. Small firms in large markets should have the potential for high growth (at least in revenues) over long periods. When looking at the size of the firm, you should look not only at its current market share, but also at the potential growth in the total market for its products or services. A firm may have a large market share of its current market, but it may be able to grow in spite of this because the entire market is growing rapidly.
2. Existing growth rate and excess returns. Momentum does matter, when it comes to projecting growth. Firms that have been reporting rapidly growing revenues are more likely to see revenues grow rapidly at least in the near future. Firms that are earning high returns on capital and high excess returns in the current period are likely to sustain these excess returns for the next few years.
3. Magnitude and sustainability of competitive advantages. This is perhaps the most critical determinant of the length of the high growth period. If there are significant barriers to entry and sustainable competitive advantages, firms can maintain high growth for longer periods. If, on the other hand, there are no or minor barriers to entry, or if the firm's existing competitive advantages are fading, you should be far more conservative about allowing for long growth periods. The quality of existing management also influences growth. Some top managers have the capacity to make the strategic choices that increase competitive advantages and create new ones. ${ }^{2}$

## competitive advantage peridd (CAP)

The confluence of high growth and excess returns that is the sozaco alue has led to the coining of the term competitive advantage period (CAP) to capture the joint effect. This term, popularized by Michael Mauboussin at Credit Suisse First Boston, measures the period for which a firm can be expected to earn excess returns. The value of such a firm can then be written as the sum of the capital invested today and the present value of the excess returns that the firm will earn over its life. Since there are no excess returns after the competitive advantage period, there is no additional value added.

In an inventive variant, analysts sometimes try to estimate how long the competitive advantage period will have to be to sustain a current market value, assuming that the current return on capital and cost of capital remain unchanged. The resulting market implied competitive advantage period (MICAP) can then be either compared across firms in a sector or evaluated on a qualitative basis.

[^1]
## ILLUSTRATION 12.1: Length of High Growth Period

To illustrate the process of estimating the length of the high growth period, we will consider a number of companies and make subjective judgments about how long each one will be able to maintain high growth:

## Consolidated Edison

Background: The firm has a monopoly in generating and selling power in the environs of New York. In return for the monopoly, though, the firm is restricted in both its investment policy and its pricing policy. A regulatory commission determines how much Con Ed can raise prices and it makes this decision based on the returns made by Con Ed on its investments; if the firm is making high returns on its investments, it is unlikely to be allowed to increase prices. Finally, the demand for power in New York is stable, as the population levels off.

Implication: The firm is already a stable growth firm. There is little potential for either high growth or excess returns.

## Procter \& Gamble

Background: Procter \& Gamble comes in with some obvious strengths. Its valuable brand names have allowed it to earn high excess returns (as manifested in its high return on equity of $29.37 \%$ in 2000 ) and sustain high growth rates in earnings over the past few decades. The firm faces two challenges. One is that it has a significant market share in a mature market in the United States, and that its brand names are less recognized and therefore less likely to command premiums abroad. The other is the increasing assault on brand names in general by generic manufacturers.

Implication: Brand name can sustain excess returns and growth higher than the stable growth rate for a short period-we will assume five years. Beyond that, we will assume that the firm will be in stable growth albeit with some residual excess returns. If the firm is able to extend its brand names overseas, its potential for high growth will be significantly higher.

## Amgen

Background: Amgen has a stable of drugs, on which it has patent protection, that generate cash flows currently, and several drugs in its R\&D pipeline. While it is the largest biotechnology firm in the world, the market for biotechnology products is expanding significantly and will continue to do so. Finally, Amgen has had a track record of delivering high earnings growth.
Implication: The patents that Amgen has will protect it from competition, and the long lead time to drug approval will ensure that new products will take a while getting to the market. We will allow for 10 years of high growth and excess returns.

There is clearly a strong subjective component to making a judgment on how long high growth will last. Much of what was said about the interrelationships between qualitative variables and growth toward the end of Chapter 11 has relevance for this discussion as well.

Characteristics of Stable Growth Firm As firms move from high growth to stable growth, you need to give them the characteristics of stable growth firms. A firm in stable growth is different from that same firm in high growth on a number of dimensions. In general, you would expect stable growth firms to have average risk, use more debt, have lower (or no) excess returns, and reinvest less than high growth firms. In this section, we will consider how best to adjust each of these variables.

Equity Risk When looking at the cost of equity, high growth firms tend to be more exposed to market risk (and have higher betas) than stable growth firms. Part of the reason for this is that they tend to be niche players supplying discretionary products, and part of the reason is high operating leverage. Thus, young technology or telecomm firms will have high betas. As these firms mature, you would expect them to have less exposure to market risk and betas that are closer to 1 -the average for the market. One option is to set the beta in stable growth to one for all firms, arguing that firms in stable growth should all be average risk. Another is to allow for small differences to persist even in stable growth with firms in more volatile businesses having higher betas than firms in stable businesses. We would recommend that, as a rule of thumb, stable period betas not exceed 1.2. ${ }^{3}$

But what about firms that have betas well below 1, such as commodity companies? If you are assuming that these firms will stay in their existing businesses, there is no harm in assuming that the beta remains at existing levels. However, if your estimates of growth in perpetuity will require them to branch out into other business, you should adjust the beta upward toward $1 .{ }^{4}$
betas.xls: This dataset on the Weh summarizes the average levered and unlevered betas, by Industry group, for flrms in the United States.

Project Returns High-growth firms tend to have high returns on capital (and equity) and earn excess returns. In stable growth, it becomes much more difficult to sustain excess returns. There are some who believe that the only assumption consistent with stable growth is to assume no excess returns; the return on capital is set equal to the cost of capital. While, in principle, excess returns in perpetuity are not feasible, it is difficult in practice to assume that firms will suddenly lose the capacity to earn excess returns. Since entire industries often earn excess returns over long periods, assuming a firm's returns on equity and capital will move toward industry averages will yield more reasonable estimates of value.
eva.xls: This dataset on the Web summarizes the returns on capital (equity), cosis of capital (equity), and excess returns, by industry group, for firms in the United States.

Debt Ratios and Costs of Debt High growth firms tend to use less debt than stable growth firms. As firms mature, their debt capacity increases. When valuing firms, this will change the debt ratio that we use to compute the cost of capital. When valuing equity, changing the debt ratio will change both the cost of equity and the expected cash flows. The question of whether the debt ratio for a firm should

[^2]be moved toward a more sustainable level in stable growth cannot be answered without looking at the incumbent managers' views on debt, and how much power stockholders have in these firms. If managers are willing to change their financing policy, and stockholders retain some power, it is reasonable to assume that the debt ratio will move to a higher level in stable growth; if not, it is safer to leave the debt ratio at existing levels.

As carnings and cash flows increase, the perceived default risk in the firm will also change. A firm that is currently losing $\$ 10$ million on revenues of $\$ 100$ million may be rated $B$, but its rating should be much better if your forecasts of $\$ 10$ billion in revenues and $\$ 1$ billion in operating income come to fruition. In fact, internal consistency requires that you reestimate the rating and the cost of debt for a firm as you change its revenues and operating income.

On the practical question of what debt ratio and cost of debt to use in stable growth, you should look at the financial leverage of larger and more mature firms in the industry. One solution is to use the industry average debt ratio and cost of debt as the debt ratio and cost of debt for the firm in stable growth.
wacc.xls: This dataset on the Weh summarizes the debt ratios and costs of debt, by industry group, for firms in the United States.

Reinvestment and Retention Ratios Stable growth firms tend to reinvest less than high-growth firms, and it is critical that we capture the effects of lower growth on reinvestment and that we ensure that the firm reinvests enough to sustain its stable growth rate in the terminal phase. The actual adjustment will vary depending on whether we are discounting dividends, free cash flows to equity, or free cash flows to the firm.

In the dividend discount model, note that the expected growth rate in earnings per share can be written as a function of the retention ratio and the return on equity.

## Expected growth rate $=$ Retention ratio $\times$ Return on equity

Algebraic manipulation can allow us to state the retention ratio as a function of the expected growth rate and return on equity:

$$
\text { Retention ratio }=\text { Expected growth rate/Return on equity }
$$

If we assume, for instance, a stable growth rate of 5 percent (based on the growth rate of the economy) for Procter \& Gamble (P\&G) and a return on equity of 15 percent, based on industry averages), we would be able to compute the retention ratio that the firm in stable growth:

$$
\text { Retention ratio }=5 \% / 15 \%=33.33 \%
$$

Procter \& Gamble will have to reinvest 33.33 percent of its earnings into the firm to generate its expected growth of 5 percent; it can pay out the remaining 66.67 percent.

In a free cash flow to equity model, where we are focusing on net income growth, the expected growth rate is a function of the equity reinvestment rate, and the return on equity:

Expected growth rate $=$ Equity reinvestment rate $\times$ Return on equity
The equity reinvestment rate can then be computed as follows:

$$
\text { Equity reinvestment rate }=\text { Expected growth rate/Return on equity }
$$

If, for instance, we assume that Coca-Cola will have a stable growth rate of 5.5 percent and that its return on equity in stable growth of 18 percent, we can estimate an equity reinvestment rate:

$$
\text { Equity reinvestment rate }=5.5 \% / 18 \%=30.56 \%
$$

Finally, looking at free cash flows to the firm, we estimated the expected growth in operating income as a function of the return on capital and the reinvestment rate:

Expected growth rate $=$ Reinvestment rate $\times$ Return on capital
Again, algebraic manipulation yields the following measure of the reinvestment rate in stable growth:

Reinvestment rate in stable growth $=$ Stable growth rate $/$ ROC $_{n}$
where the $R O C_{n}$ is the return on capital that the firm can sustain in stable growth. This reinvestment rate can then be used to generate the free cash flow to the firm in the first year of stable growth.

Linking the reinvestment rate retention ratio to the stable growth rate also makes the valuation less sensitive to assumptions about the stable growth rate. While increasing the stable growth rate, holding all else constant, can dramatically increase value, changing the reinvestment rate as the growth rate changes will create an offsetting effect. The gains from increasing the growth rate will be partially or completely offset by the loss in cash flows because of the higher reinvestment rate. Whether value increases or decreases as the stable growth increases will entirely depend on what you assume about excess returns. If the return on capital is higher than the cost of capital in the stable growth period, increasing the stable growth rate will increase value. If the return on capital is equal to the stable growth rate, increasing the stable growth rate will have no effect on value. This can be proved quite easily:

$$
\text { Terminal value }=\frac{E_{B I T}^{n+1}}{}(1-t)(1-\text { Reinvestment rate })
$$

Substituting in the stable growth rate as a function of the reinvestment rate, from the equation, you get:

$$
\text { Terminal value }=\frac{\operatorname{EBIT}_{n+1}(1-t)(1-\text { Reinvestment rate })}{\text { Cost of capital }-(\text { Reinvestment rate } \times \text { Return on capital })}
$$

Setting the return on capital equal to the cost of capital, you arrive at:

$$
\text { Terminal value }=\frac{\operatorname{EBIT}_{\mathrm{n}+1}(1-\mathrm{t})(1-\text { Reinvestment rate })}{\text { Cost of capital }}
$$

Simplifying, the terminal value can be stated as:

$$
\text { Terminal value }{ }_{\mathrm{ROC}=\mathrm{WACC}}=\frac{\operatorname{EBIT}_{\mathrm{n}+1}(1-\mathrm{t})}{\text { Cost of capital }}
$$

You could establish the same proposition with equity income and cash flows, and show that a return on equity equal to the cost of equity in stable growth nullifies the positive effect of growth.
divtund.xis: This dataset on the Web summarizes retention ratios, by industry group, for firms in the United States.
capex.xls: This dataset on the Web summarizes the reinvestment rates, by industry group, for firms in the United States.

## ILLUSTRATION 12.2: Stable Growth Rates and Excess Returns

Alloy Mills is a textile firm that is cursently reporting after-tax operating income of $\$ 100$ million. The firm has a return on capital currently of $20 \%$ and reinvests $50 \%$ of its earnings back into the firm, giving if an expected growth rate of $10 \%$ for the next five years:

$$
\text { Expected growth rate }=20 \% \times 50 \%=10 \%
$$

After year 5 the growth rate is expected to drop to $5 \%$ and the return on capital is expected to stay at $20 \%$. The terminal value can be estimated as follows:

Expected operating income in year $6=100(1.10)^{5}(1.05)=\$ 169.10$ million
Expected reinvestment rate from year $5=g / R O C=5 \% / 20 \%=25 \%$
Terminal value in year $5=\$ 169.10(1-.25) /(.10-.05)=\$ 2,537$ million
The value of the firm today would then be:

$$
\begin{aligned}
\text { Value of firm today }= & \$ 55 / 1 \cdot 10+\$ 60.5 / 1.10^{2}+\$ 66.55 / 1.10^{3}+\$ 73.21 / t \cdot 10^{4} \\
& +\$ 80.53 / 1.10^{5}+\$ 2,537 / 1.10^{5}=\$ 2,075 \text { million }
\end{aligned}
$$

If we did change the return on capital in stable growth to $10 \%$ while keeping the growth rate at $5 \%$, the effect on value would be dramatic:

Expected operating income in year $6=100(1.10)^{5}(1.05)=\$ 169.10$ million
Expected reinvestment rate from year $5=\mathrm{g} / \mathrm{ROC}=5 \% / 10 \%=50 \%$
Terminal value in year $5=\$ 169.10(1-.5) /(.10-.05)=\$ 1,691$ million
Value of firm today $=\$ 55 / 1.10+\$ 60.5 / 1.10^{2}+\$ 66.55 / 1.10^{3}+\$ 73.21 / 1.10^{4}$

$$
+\$ 80.53 / 1.10^{5}+\$ 1,69 \dagger / 1.10^{5}=\$ 1,300 \text { million }
$$

Now consider the effect of lowering the growth rate to $4 \%$ while keeping the return on capital at $10 \%$ in stable growth:

Expected operating income in jear $6=100(1.10)^{5}(1.04)=\$ 167.49$ million
Expected reinvestment rate in jear $6=g$ ROC $=4 \% .10 \%=40 \%$
Terminal value in year $5=\$ 167.49(1-.4) /(10-.04)=\$ 1,675$ milion
Value of firm today $=\$ 55 / 1.10+\$ 60.5 / 1.10^{2}+\$ 66.55 / 1.10^{3}+\$ 73.21 / 1.10^{4}$
$+\$ 96.63 / 1.10^{5}+\$ 1,675 / 1.10^{5}=\$ 1,300$ million
Note that the terminal value decreases by $\$ 16$ million but the cash flow in year 5 also increases by $\$ 16$ million because the reinvestment rate at the end of year 5 drops to $40 \%$. The value of the firm remains unchanged at $\$ 1,300$ million. In fact, changing the stable growth rate to $0 \%$ thas no effect on value:

Expected operating income in year $6=100(1.10)^{5}=\$ 161.05$ million
Expected reinvestment rate in year $6=g /$ ROC $=0 \% / 10 \%=0 \%$
Terminal value in year $5=\$ 161.05(1-.0) /(.10-.0)=\$ 1.610 .5$ million
Value of firm today $=\$ 55 / 1.10+\$ 60.5 / 1.10^{2}+\$ 66.55 / 1.10^{3}+\$ 73.21 / 1.10^{4}$
$+\$ 161.05 / \mathrm{t} \cdot 10^{5}+\$ 1,610.5 / 1.10^{5}=\$ 1,300$ million

## ILLUSTRATION 12.3: Stable Growth Inputs

To illustrate how the inputs to valuation change as we go from high growth to stable growth, we will consider three firms-Procter \& Gamble, with the dividend discount model; Coca-Cola, with a free cash flow to equity model; and Embraer, the Brazilian aerospace firm with a free cash flow to firm model.

Consider Procter \& Gamble first in the context of the dividend discount model. While we will do the valuation in the next chapter, note that there are only three real inputs to the dividend discount model-the payout ratio (which determines dividends), the expected return on equity (which determines the expected growth rate), and the beta (which affects the cost of equity). In IIIustration 12.1, we argued that Procter \& Gamble would have a five-year high-growth period. The following table summarizes the inputs into the dividend discount model for the valuation of Procter \& Gamble.

Payout ratio
Return on equity
Expected growth rate Beta

| High Growth Period | Stable Growth Period |
| :---: | :---: |
| $45.67 \%$ | $66.67 \%$ |
| $25.00 \%$ | $15.00 \%$ |
| $13.58 \%$ | $5.00 \%$ |
| 0.85 | 1.00 |

Note that the payout ratio and the beta for the high-growth period are based on the current year's values. The return on equity for the next five years is set at $25 \%$, which is below the current return on equity but reflects the competitive pressures that Procter \& Gamble has been under recently. The expected growth rate of $13.58 \%$ for the next five years is the product of the return on equity and retention ratio. In stable growth, we adjust the beta to one, though the adjustment has
little effect on value since the beta is already close to 1 . We assume that the stable growth rate will be $5 \%$, just slightly below the nominal growth rate in the global economy. We also assume that the return on equity will drop to $15 \%$, about halfway between the cost of equity and the average return on equity earned by brand-name companies similar to Procter \& Gamble today. This reflects our assumption that returns on equity will decline for the entire industry as competition from generics eats into profit margins. The retention ratio decreases to $33.33 \%$, as both growth and return on equity drop.

To analyze Coca-Cola in a free cash flow to equity model, the following table summarizes our inputs for high growth and stable growth:

|  | High Growth | Stable Growth |
| :--- | :---: | :---: |
| Return on equity | $27.83 \%$ | $20.00 \%$ |
| Equity reinvestment rate | $39.32 \%$ | $27.50 \%$ |
| Expected growth | $10.94 \%$ | $5.50 \%$ |
| Beta | 0.8 | 0.80 |

In high growth, the high equity reinvestment rate and high return on equity combine to generate an expected growth rate of $10.94 \%$ a year. In stable growth, we reduce the return on equity for Coca-Cola to the industry average for beverage companies and estimate the expected equity reinvestment rate based on a stable growth rate of $5.5 \%$. The beta for the firm is left unchanged at its existing level, since Coca-Cola's management has been fairly disciplined in staying focused on the core businesses.

Finally, let us consider Amgen. The following table reports on the return on capital, reinvestment rate, and debt ratio for the firm in high growth and stable growth periods.

|  | High Growth | Stable Growth |
| :--- | :---: | :---: |
| Return on capital | $23.24 \%$ | $20.00 \%$ |
| Reinvestment rate | $56.27 \%$ | $25.00 \%$ |
| Expected growth | $13.08 \%$ | $5.00 \%$ |
| Beta | 1.35 | 1.00 |

The firm has a high return on capital currently, and we assume that this return will decrease slightly in stable growth to $20 \%$ as the firm becomes larger and patents expire. Since the stable growth rate drops to $5 \%$, the resulting reinvestment rate at Amgen will decrease to $25 \%$. We will also assume that the beta for Amgen will converge on the market average.

For all of the firms, it is worth noting that we are assuming that excess returns continue in perpetuity by setting the return on capital above the cost of capital. While this is potentially troublesome, the competitive advantages that these firms have builk up historically or will build up over the highgrowth phase will not disappear in an instant. The excess returns will fade over time, but moving them to or toward industry averages in stable growth seems like a reasonable compromise.

Transition to Stable Growth Once you have decided that a firm will be in stable growth at a point in time in the future, you have to consider how the firm will change as it approaches stable growth. There are three distinct scenarios. In the first, the firm will be maintain its high growth rate for a period of time and then become a stable growth firm abruptly; this is a two-stage model. In the second, the firm will maintain its high growth rate for a period and then have a transition period where its characteristics change gradually toward stable growth levels; this is a three-stage model. In the third, the firm's characteristics change each year from the initial period to the stable growth period; this can be considered an n-stage model.

Which of these three scenarios gets chosen depends on the firm being valued. Since the firm goes in one year from high growth to stable growth in the twostage model, this model is more appropriate for firms with moderate growth rates, where the shift will not be too dramatic. For firms with very high growth rates in operating income, a transition phase allows for a gradual adjustment not just of growth rates but also of risk characteristics, returns on capital and reinvestment rates towards stable growth levels. For very young firms or for firms with negative operating margins, allowing for changes in each year (in an nstage model) is prudent.

## ILLUSTRATION 12.4: Choosing a Growth Pattern

Consider the three firms analyzed in Illustration 12.3. We assumed a growth rate of $13.58 \%$ and a high-growth period of five years for P\&G, a growth rate of $10.94 \%$ and a high-growth period of 10 years for Coca-Cola, and a growth rate of $13.08 \%$ and a high-growth period of 10 years for Amgen. For Procter \& Gamble, we will use a two-stage model-growth of $13.58 \%$ for five years and $5 \%$ thereafter. For both Coca-Cola and Amgen, we will allow for a transition phase between years 6 and 10 where the inputs will change gradually from high growth to stable growth levels. Figure 12.1 reports on how the payout ratio and expected growth change at Coca-Cola, from years 6 through 10, as well as the change in the return on capital and reinvestment rate at Amgen over the same period.


FIEURE 12.1 Fundamentals and Growth in Transition

## EXtraordinary browth periods without a hith growth rate or a megative growit rate

Can you have extraordinary growth periods for firms that bave expected growth rates that are less than or equal to the growth rate of the economy? The answer is yes, for some firms. This is because stable growth requires not just that the growth rate be less than the growth rate of the economy, but that the other inputs into the valuation are also appropriate for a stable growth firm. Consider, for instance, a firm whose operating income is growing at 4 percent a year but whose current return on capital is 20 percent and whose beta is 1.5 . You would still need a transition period where the return on capital declined to more sustainable levels (say 12 percent) and the beta moved toward 1.

By the same token, you can have an extraordinary growth period, where the growth rate is less than the stable growth rate and then moves up to the stable growth rate. For instance, you could have a firm that is expected to see its earnings grow at 2 percent a year for the next five years (which would be the extraordinary growth period) and 5 percent thereafter.

## the survival issue

Implicit in the use of a terminal value in discounted cash flow valuation is the assumption that the value of a firm comes from it being a going concern with a perpetual life. For many risky firms, there is the very real possibility that they might not be in existence in 5 or 10 years, with volatile earnings and shifting technology. Should the valuation reflect this chance of failure, and, if so, how can the likelihood that a firm will not survive be built into a valuation?

## LIfe Cycle and Firm Survival

There is a link between where a firm is in the life cycle and survival. Young firms with negative earnings and cash flows can run into serious cash flow problems and: end up being acquired by firms with more resources at bargain basement prices. Why are young firms more exposed to this problem? The negative cash flows from operations, when combined with significant reinvestment needs, can result in a rapid depletion of cash reserves. When financial markets are accessible and additional equity (or debr) can be raised at will, raising more funds to meet these funding needs is not a problem. However, when stock prices drop and access to markets becomes more limited, these firms can be in trouble.

A widely used measure of the potential for a cash flow problem for firms with negative earnings is the cash burn ratio, which is estimated as the cash balance of the firm divided by its earnings before interest, taxes, depreciation, and amortization (EBITDA).
where EBITDA is a negative number and the absolute value of EBITDA is used to estimate this ratio. Thus a firm with a cash balance of $\$ 1$ billion and EBITDA of $-\$ 1.5$ billion will burn through its cash balance in eight months.

## Likellhood of Fallure and Valuation

One view of survival is that the expected cash flows that you use in a valuation reflect cash flows under a wide range of scenarios from very good to abysmal and the probabilities of the scenarios occurring. Thus, the expected value already has built into it the likelihood that the firm will not survive. Any market risk associated with survival or failure is assumed to be incorporated into the cost of capital. Firms with a high likelihood of failure will therefore have higher discount rates and lower present values.

Another view of survival is that discounted cash flow valuations tend to have an optimistic bias and that the likelihood that the firm will not survive is not considered adequately in the value. With this view, the discounted cash flow value that emerges from the analysis in the prior section overstates the value of operating assets and has to be adjusted to reflect the likelihood that the firm will not survive to deliver its terminal value or even the positive cash flows that you have forecast in future years.

## Should You op 8hould You Nat Dlscount Value for Survival?

For firms that have substantial assets in place and relatively small probabilities of distress, the first view is the more appropriate one. Attaching an extra discount for nonsurvival is double counting risk.

For younger and smaller firms, it is a tougher call and depends on whether expected cash flows consider the probability that these firms may not make it past the first few years. If they do, the valuation already reflects the likelihood that the firms will not survive past the first few years. If they do not, you do have to discount the value for the likelihood that the firm will not survive the near future. One way to estimate this discount is to use the cash burn ratio, described earlier, to estimate a probability of failure, and adjust the operating asset value for this probability:

$$
\begin{aligned}
\text { Adjusted value }= & \text { Discounted cash flow value }(1-\text { Probability of distress) } \\
& + \text { Distressed sale value(Probability of distress) }
\end{aligned}
$$

For a firm with a discounted cash flow value of $\$ 1$ billion on its assets, a distress sale value of $\$ 500$ million and a 20 percent probability of distress, the adjusted value would be $\$ 900$ million:

$$
\text { Adjusted value }=\$ 1,000(.8)+\$ 500(.2)=\$ 900 \text { million }
$$

There are two points worth noting here. It is not the failure to survive per se that causes the loss of value but the fact that the distressed sale value is at a discount on the true value. The second is that this approach revolves around estimating the probability of failure. This probability is difficult to estimate because it will depend upon both the magnitude of the cash reserves of the firm (relative to its cash needs) and the state of the market. In buoyant equity markets, even firms with little or no cash can survive because they can access markets for more funds. Under more negative market conditions, even firms with significant cash balances may find themselves under threat.

## ESTIMATING THE PROBABILITY OF DISTRESS

There are two ways in which we can estimate the probability that a firm will not survive. One is to draw un the past, look at firms that have failed, wiupare them to frms hat did not, and look for variables that seem to set them apart. For inceamcs, firms with high debt ratios and negative cash flows from operations may be more likely to fail than firms without these characteristics. In fact, you can use statistical techniques such as probits to estimate the probability that a firm will fail. To run a probit, you would begin, for instance, with all listed firms in 1990 and their financial characteristics, identify the firms that failed during the 1991-1999 time period and then estimate the probability of failure as a function of variables that were observable in 1990. The output, which resembles regression output, will then let you estimate the probability of default for any firm today.

The other way of estimating the probability of default is to use the bond rating for the firm, if it is available. For instance, assume that Commerce One has a B rating. An empirical examination of B-rated bonds over the past few decades reveals that the likelihood of defaule withe this rat ng is 25 percent. ${ }^{5}$ While this approact rated firms, and it : 1 be used only for ndards used by ratings agencies have not changed significantly over tume.

## CLOSING THOUGHTS ON TERMINAL VALUE

The role played by the terminal value in discounted cash flow valuations has often been the source of much of the criticism of the discounted cash flow approach. Critics of the approach argue that too great a proportion of the discounted cash flow value comes from the terminal value and that it is easy to manipulate the terminal value to yield any number you want. They are wrong on both counts.

It is true that a large portion of the value of any stock or equity in a business comes from the terminal value, but it would be surprising if it were not so. When you buy a stock or invest in the equity in a business, consider how you get your returns. Assuming that your investment is a good investment, the bulk of the returns come not while you hold the equity (from dividends or other cash flows) but when you sell it (from price appreciation). The terminal value is designed to capture the latter. Consequently, the greater the growth potential in a business, the higher the proportion of the value that comes from the terminal value.

Is it easy to manipulate the terminal value? We concede that terminal value is manipulated often and easily, but it is because analysts either use multiples to get these values or because they violate one or both of two basic propositions in stable growth models. One is that the growth rate cannot exceed the growth rate of the

[^3]economy. The other is that firms have to reinvest in stable growth to generate the growth rate. In fact, as we showed earlier in the chapter, it is not the stable growth rate that drives value as much as what we assume about excess returns in perpetuity. When excess returns are zero, changes in the stable growth rate have no impact on value.

## CONCLUSION

The value of a firm is the present value of its expected cash flows over its life. Since firms have infinite lives, you apply closure to a valuation by estimating cash flows for a period and then estimating a value for the firm at the end of the period-a terminal value. Many analysts estimate the terminal value using a multiple of earnings or revenues in the final estimation year. If you assume that firms have infinite lives, an approach that is more consistent with discounted cash flow valuation is to assume that the cash flows of the firm will grow at a constant rate forever beyond a point in time. When the firm that you are valuing will approach this growth rate, which you label a stable growth rate, is a key part of any discounted cash flow valuation. Small firms that are growing fast and have significant competitive advantages should be able to grow at high rates for much longer periods than larger and more mature firms, without these competitive advantages. If you do not want to assume an infinite life for a firm, you can estimate a liquidation value based on what others will pay for the assets that the firm has accumulated during the high-growth phase.

## qUESTIONS AND SHORT PROBLEMS

1. Ulysses Inc. is a shipping company with $\$ 100$ million in earnings before interest and taxes that is expected to have earnings growth of $10 \%$ for the next five years. At the end of the fifth year, you estimate the terminal value using a multiple of 8 times operating income (which is the average for the sector).
a. Estimate the terminal value of the firm.
b. If the cost of capital for Ulysses is $10 \%$, the tax rate is $40 \%$, and you expect the stable growth rate to be $5 \%$, what is the return on capital that you are assuming in perpetuity if you use a multiple of 8 times operating income.
2. Genoa Pasta manufactures Italian food products and currently earns $\$ 80$ million in earnings before interest and taxes. You expect the firm's earnings to grow 20 percent a year for the next six years and $5 \%$ thereafter. The firm's current aftertax return on capital is $28 \%$, but you expect it to be halved after the sixth year. If the cost of capital for the firm is expected to be $10 \%$ in perpetuity, estimate the terminal value for the firm. (The tax rate for the firm is $40 \%$.)
3. Lamps Galore Inc. manufactures table lamps and earns an after-tax return on capital of $15 \%$ on its current capital invested (which is $\$ 100$ million). You expect the firm to reinvest $80 \%$ of its after-tax operating income back into the business for the next four years and $30 \%$ thereafter (the stable growth period). The cost of capital for the firm is $9 \%$.
a. Estimate the terminal value for the firm (at the end of the fourth year).
b. If you expected the after-tax return on capital to drop to $9 \%$ after the fourth year, what would your estimate of terminal value be?
4. Bevan Real Estate Inc. is a real estate holding company with four properties. You estimate that the income from these properties, which is currently $\$ 50$ million after taxes, will grow $8 \%$ a year for the next 10 years and $3 \%$ thereafter. The current market value of the properties is $\$ 500$ million, and you expect this value to appreciate at $3 \%$ a year for the next 10 years.
a. Estimate the terminal value of the properties, based on the current market value and the expected appreciation rate in property values.
b. Assuming that your projections of income growth are right, what is the terminal value as a multiple of after-tax operating income in the tenth year?
c. If you assume that no reinvestment is needed after the tenth year, estimate the cost of capital that you are implicitly assuming with your estimate of the terminal value.
5. Latin Beats Corporation is a firm that specializes in Spanish music and videos. In the current year, the firm reported $\$ 20$ million in after-tax operating income, $\$ 15$ million in capital expenditures, and $\$ 5$ million in depreciation. The firm expects all three items to grow at $10 \%$ for the next five years. Beyond the fifth year, the firm expects to be in stable growth and grow at $4 \%$ a year in perpetuity. You assume that earnings, capital expenditures, and depreciation will grow at $4 \%$ in perpetuity and that your cost of capital is $12 \%$. (There is no working capital.)
a. Estimate the terminal value of the firm.
b. What reinvestment rate and return and capital are you implicitly assuming in perpetuity when you do this?
c. What would your terminal value have been if you had assumed that capital expenditures offset depreciation in stable growth?
d. What return on capital are you implicitly assuming in perpetuity when you set capital expenditures equal to depreciation?
6. Crabbe Steel owns a number of steel plants in Pennsylvania. The firm reported after-tax operating income of $\$ 40$ million in the most recent year on capital invested of $\$ 400$ million. The firm expects operating income to grow $7 \%$ a year for the next three years, and $3 \%$ thereafter
a. If the firm's cost of capital is $10 \%$ and you expect the firm's current return on capital to continue in perpetuity, estimate the value at the end of the third year.
b. If you expect operating income to stay fixed after year 3 (what you earn in year 3 is what you will earn every year thereafter), estimate the terminal value.
c. If you expect operating income to drop $5 \%$ a year in perpetuity after year 3 , estimate the terminal value.
7. How would your answers to the preceding problem change if you were told that the cost of capital for the firm is $8 \%$ ?

[^0]:    'Growth without excess returns will make a firm larger but not add value.

[^1]:    ${ }^{2}$ Jack Welch at GE and Roberto Goizueta at Coca-Cola are good examples of CEOs who made a profound difference in the growth of their firms.

[^2]:    ${ }^{3}$ Two-thirds of U.S. firms have betas that fall between 0.8 and 1.2. That becomes the range for stable period betas.
    ${ }^{4}$ If you are valuing a commodity company and assuming any growth rate that exceeds inflation, you are assuming that your firm will branch into other businesses and you have to adjust the beta accordingly.

[^3]:    ${ }^{\text {s Professor Altman at NYU's Stern School of Business estimates these probabilities as part of }}$ an annual series that he updates. The latest version is available from the Stern School of Business working paper series.

